

Essential Outcome	Lesson/Video	Practice Questions
Construct a linear equation given a table of values	Method 1: <a href="https://www.youtube.com/watch?v=9wixvKtebbE">https://www.youtube.com/watch?v=9wixvKtebbE</a>  Method 2: (Slope-Intercept Form) <a href="https://www.youtube.com/watch?v=o09bdHA5ZBA">https://www.youtube.com/watch?v=o09bdHA5ZBA</a>	<a href="#">Worksheet #1: Constructing a Linear Equation from a Table of Values</a>
Construct linear equations from context.  Identify a pattern in a problem and use it to interpolate and extrapolate data.	Notes to Accompany Video 1 are <a href="#">below</a> in this document.  Video 1: <a href="https://youtu.be/7JU8nbatt9A">https://youtu.be/7JU8nbatt9A</a>  Video 2: <a href="https://youtu.be/hBpl9lfmMKg">https://youtu.be/hBpl9lfmMKg</a>	<a href="#">Worksheet #2: Word Problems</a>

Worksheet #1: Constructing a Linear Equation from a Table of Values

Write the equation represented by each table of values.

1.

x	y
-2	2
-1	3
0	4
1	5
2	6

2.

x	y
-5	6
-4	4
-3	2
-2	0
-1	-2

3.

x	y
-6	-6
-5	-3
-4	0
-3	3
-2	6

4.

x	y
0	8
1	6
2	4
3	2
4	0

5.

x	y
0	8
2	6
4	4
6	2
8	0

6.

x	y
0	0
1	-4
2	-8
3	-12
4	-16

**Answers:**

- $y = x + 4$**
- $y = -2x - 4$**
- $y = 3x + 12$**
- $y = -2x + 8$**
- $y = -x + 8$**
- $y = -4x$**

Notes: How to construct linear equations from context, identify a pattern in a problem, and extrapolate data.

**Example to Accompany Instructional Video:**

Apolline is mowing lawns for a summer job. For every mowing job, she charges an initial fee of \$7 plus a constant fee for each hour of work. Her fee for a 5-hour job, for instance, is \$42. Her fee for a 3-hour job is \$28.

Let  $y$  represent Apolline's fee (in dollars) for a single job that took  $x$  hours for her to complete.

**A. Complete the equation for the relationship between the fee and number of hours worked using the steps below.**

- Create a table of values

x (hours)	y (fee)
3	\$28
5	\$42

- Find slope  $\left(\frac{\text{Change in } y}{\text{Change in } x}\right)$

x (hours)	y (fee)
3	\$28
5	\$42

+2      +14

$$\text{slope } (m) = \left(\frac{\text{Change in } y}{\text{Change in } x}\right)$$

$$\text{slope } (m) = \left(\frac{14}{2}\right)$$

$$\text{slope } (m) = 7$$

- Find y-intercept (What is the value of  $y$  when  $x=0$  on the table)

x (hours)	y (fee)
0	\$7 initial fee
3	\$28
5	\$42

**OR**, you can substitute any known point and the slope into the slope-intercept equation and solve for  $b$  to find the intercept. I chose the point (3,28)

$$y = mx + b$$

$$28 = 7(3) + b \text{ (substitute } y=28, m=7, \text{ and } x=3)$$

$$28 = 21 + b$$

$$28 - 21 = 21 - 21 + b$$

$$7 = b$$

- Plug in the values for slope and the y-intercept into slope-intercept form of an equation. ( $y=mx+b$ , where  $m$  = slope and  $b$  = y-intercept)

$$y = mx + b$$

$$y = 7x + 7$$

**B. How many hours would she have worked if she made \$63?**

$$y = 7x + 7$$

$$63 = 7x + 7$$

$$63 - 7 = 7x + 7 - 7$$

$$56 = 7x$$

$$\frac{56}{7} = \frac{7x}{7}$$

$$8 = x$$

Substitute  $y = 63$  into the equation and solve for  $x$

She would have worked 8 hours if she made \$63.

**C. How much money would she make for working 6 hours?**

$$y = 7x + 7$$

$$y = 7(6) + 7$$

$$y = 42 + 7$$

$$y = 49$$

Substitute  $x = 6$  into the equation and solve for  $y$

She would make \$49 if she worked 6 hours.

## Worksheet #2: Word Problems

### Problem #1:

A lake near the Arctic Circle is covered by a 2-meter-thick sheet of ice during the cold winter months. When spring arrives, the warm air gradually melts the ice, causing its thickness to decrease at a constant rate. After 3 weeks, the sheet is only 1.25 meters thick.

Let  $y$  represent the ice sheet's thickness (in meters) after  $x$  weeks.

- A. Complete the equation for the relationship between the thickness and number of weeks using the steps below.
- Create a table of values
  - Find slope  $\left(\frac{\text{Change in } y}{\text{Change in } x}\right)$
  - Find  $y$ -intercept (What is the value of  $y$  when  $x=0$  on the table)
  - Plug in the values for slope and the  $y$ -intercept into slope-intercept form of an equation. ( $y=mx+b$ , where  $m$ =slope and  $b$ =  $y$ -intercept)
- B. How much ice will be left after 6 weeks?
- C. How long will it take for the ice to disappear?

### Problem #2:

Mr. Mole left his burrow that lies 7 meters below the ground and started digging his way deeper into the ground, descending at a constant rate. After 6 minutes, he was 16 meters below the ground.

Let  $y$  represent Mr. Mole's altitude (in meters) relative to the ground after  $x$  minutes.

- A. Complete the equation for the relationship between the altitude and number of minutes using the steps below.
- Create a table of values
  - Find slope  $\left(\frac{\text{Change in } y}{\text{Change in } x}\right)$
  - Find  $y$ -intercept (What is the value of  $y$  when  $x=0$  on the table)
  - Plug in the values for slope and the  $y$ -intercept into slope-intercept form of an equation. ( $y=mx+b$ , where  $m$ =slope and  $b$ =  $y$ -intercept)
- B. How long will it take Mr. Mole to dig 20 meters ( $y = -20$ )?
- C. What would Mr. Mole's altitude be after 12 minutes of digging?

### Problem #3:

A young sumo wrestler decided to go on a special high-protein diet to gain weight rapidly. He started at 90 kilograms and gained weight at a constant rate. After 8 months, he weighed 138 kilograms.

Let  $y$  represent the sumo wrestler's weight (in kilograms) after  $x$  months.

- A. Complete the equation for the relationship between the weight and number of months using the steps below.
- Create a table of values
  - Find slope  $\left(\frac{\text{Change in } y}{\text{Change in } x}\right)$
  - Find  $y$ -intercept (What is the value of  $y$  when  $x=0$  on the table)
  - Plug in the values for slope and the  $y$ -intercept into slope-intercept form of an equation. ( $y=mx+b$ , where  $m$ =slope and  $b$ =  $y$ -intercept)
- B. How much did he weigh 4 months into his high protein diet?
- C. How many months will it take him to reach 150kg?

### Problem #4:

Kayden is a stunt driver. One time, during a gig where she escaped from a building about to explode, she drove at a constant speed to get to the safe zone that was 160 meters away. After 3 seconds of driving, she was 85 meters away from the safe zone.

Let  $y$  represent the distance (in meters) from the safe zone after  $x$  seconds.

- A. Complete the equation for the relationship between the distance and number of seconds using the steps below.
- Create a table of values
  - Find slope  $\left(\frac{\text{Change in } y}{\text{Change in } x}\right)$
  - Find  $y$ -intercept (What is the value of  $y$  when  $x=0$  on the table)
  - Plug in the values for slope and the  $y$ -intercept into slope-intercept form of an equation. ( $y=mx+b$ , where  $m$ =slope and  $b$ =  $y$ -intercept)

- B. How long did it take her to reach the safe zone?
- C. How far past the safe zone would she be after 9 seconds of driving?

**Problem #5: (More challenging)**

Noa drove from the Dead Sea up to Jerusalem, and her altitude increased at a constant rate of 740 meters per hour. When she arrived in Jerusalem after 1.5 hours of driving, her altitude was 710 meters above sea level.

Let  $y$  represent Noa's altitude (in meters) relative to sea level after  $x$  hours.

- A. Complete the equation for the relationship between the altitude and number of hours using the steps below.
  - Create a table of values [hint: Use the rate of her increase in altitude (the slope) to add more values to your table besides the one given]
  - Extrapolate to find the  $y$ -intercept (What is the value of  $y$  when  $x=0$  on the table). In other words, what was her altitude when she began driving?
  - Plug in the values for slope and the  $y$ -intercept into slope-intercept form of an equation. ( $y=mx+b$ , where  $m$ =slope and  $b$ =  $y$ -intercept)

**Worksheet #2: Answers**

Problem #1:	Problem #2:	Problem #3:	Problem #4:	Problem #5:
A. $y = -0.25x + 2$ B. 0.5 m C. 8 weeks	A. $y = -\frac{3}{2}x - 7$ B. 8.7 minutes C. -25m (25 m underground)	A. $y = 6x + 90$ B. 114kg C. 10 months	A. $y = -25x + 160$ B. 6.4s C. 65 meters past the safe zone (or -65m)	A. $y = 740x - 400$